Quadrilateral Q_k elements and the regular decomposition property

Gabriel Acosta

University of Buenos Aires, Argentina gacosta@dm.uba.ar

Let $K \subset \mathbb{R}^2$ be a convex quadrilateral. In [1] the following definition can be found: K satisfies the regular decomposition property with constants $N < \infty$ and $0 < \psi < \pi$ if we can divide K into two triangles along one of its diagonals, called d_1 , in such a way that $|d_2|/|d_1| < N$ and the maximum angle of both triangles is bounded by ψ . Moreover, in [1] it is shown that the constant in the estimate of the H_1 norm of the error for the Q_1 -Lagrange interpolation can be bounded in terms of N and ψ . In [2] this result is generalized to $W^{1,p}$ for $1 \le p < 3$, while for $3 \le p$ it is shown that the constant can be bounded in terms of the minimal and the maximal angle of K. In this talk we show the role of the regular decomposition property in quadrilateral Q_k interpolation for $k \ge 2$.

- [1] G. Acosta, R. Duran Error estimates for Q_1 -isoparametric elements satisfying a weak angle condition. SIAM J. Numer. Anal. 38, 1073-1088, 2000.
- [2] G. Acosta, G. Monzon Interpolation error estimates in $W^{1,p}$ for degenerate Q_1 -isoparametric elements. Numer. Math. , 104, pp 129-150, 2006.

Joint work with Gabriel Monzón (Universidad de General Sarmiento, Argentina).